Accel Precalc
Unit 3: Matrices
Lesson 8

Notes: Solving Systems of Equations with Matrices

Name _____

EQ:

- ❖ Get out and cut on your graphing calculator.
- Use your graphing calculator to perform the following operation in the given matrices.

$$A = \begin{bmatrix} 5 & 7 & -3 & 0 \\ -2 & 1 & 8 & 11 \end{bmatrix} \qquad B = \begin{bmatrix} 8 & -5 & 2 & -1 \\ 4 & -2 & 0 & -5 \\ 3 & 5 & 7 & -6 \end{bmatrix} \qquad C = \begin{bmatrix} 7 \\ 2 \\ 6 \end{bmatrix} \qquad D = \begin{bmatrix} 3 & -1 & 9 & 8 \\ 6 & 2 & 0 & 5 \end{bmatrix} \quad E = \begin{bmatrix} -3 & 8 & -5 \end{bmatrix}$$

$$F = \begin{bmatrix} -4 & 8 \\ 0 & 9 \\ 5 & -3 \\ 1 & 2 \end{bmatrix}$$

a) A + D

b) CB

c) BD

d) FD

A system of equations may be represented as a matrix equation. For example, the system of equations $\begin{cases} 3x-5y=1 & \text{may be represented by the matrix equation} \\ 2x+y=-2 & \end{cases}$

- Ex. 1 Write the matrix equation that represents the system: $\begin{cases} x+y=8\\ 2x+y=1 \end{cases}$
- Ex. 2 Write the matrix equation that represents the system: $\begin{cases} x+3y=13\\ 2x-y=-9 \end{cases}$
- Ex. 3 Write the system of equations represented by the matrix equation $\begin{bmatrix} -1 & 5 & 2 \\ 1 & 2 & 0 \\ 4 & 0 & -3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -5 \\ -4 \\ 10 \end{bmatrix}$

A matrix equation is in the form AX = B, where A is the _____ matrix, X is the _____ matrix, and B is the ____ matrix.

$$\begin{bmatrix} 3 & -5 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

B = A = X =

Ex. 4 Solve each system using a matrix equation. SET UP THE CORRECT MATRIX EQUATION FOR EACH PROBLEM.

a)
$$2x+3y=2$$
 b) $4x-9y=-1$

b)
$$9x-7y=5$$
 c) $10x+3y=-16$

$$x-2y+3z=32x+y+5z=83x-y-3z=-22$$
 d)
$$5x-4y+3z=156x+2y+9z=137x+6y-6z=6$$

Ex. 5 Application Problem

A financial manager wants to invest \$50,000 for a client by putting some of the money in a low-risk investment that earns 5% per year and some of the money in a high-risk investment that earns 14% per year. How much money should she invest at each interest rate to earn \$5000 in interest per year?

$$\begin{cases}
-3x + 4y = 3 \\
-6x + 8y = 18
\end{cases}$$

Ex. 7 Solve the system using a matrix equation.
$$\begin{cases} 9x - 3y = 27 \\ -6x + 2y = -18 \end{cases}$$

$$\begin{cases} 9x - 3y = 27 \\ -6x + 2y = -18 \end{cases}$$

* Assignment: Textbook p. 589 #51 - 63 odd Use the determinant and/or matrices to solve each system. If there is not a unique solution classify the system as consistent dependent, or inconsistent.