Accel Math III Handout: Transformations of Sine \& Cosine $\qquad$
Unit \#6: Graphs and Inverses of Trig Functions Lesson \#4: Transformations of Sine and Cosine

EQ:
$>$ Recall: Transformations of Graphs of Functions
Given $y=f(x) \quad$ transformed function $y=$ $\qquad$
Where:
$\qquad$
$>$ Standard Form of Sine and Cosine Equations: $\qquad$
$y=$ $\qquad$

- Amplitude --- represented by $\qquad$ : notation $\qquad$ ; measured from the
$\qquad$ line of $\qquad$ .

Graphically --- distance from $\qquad$ line of symmetry to $\qquad$ or
$\qquad$

Algebraically ---
Find the amplitude both graphically and algebraically. Write the function represented by the graph.


Ex. 2


Graphically =
Algebraically =
Graphically =
Algebraically =

$$
y=
$$

$\qquad$

$$
y=
$$

$\qquad$

- New Period --- complete $\qquad$ on $\qquad$ or $\qquad$ using $\qquad$ from equation

RECALL: Sine and Cosine cycle every $\qquad$ or $\qquad$ radians.

Ex 3. What is the amplitude and new period for the graph below?
$|A|=$

Use graph to determine B.

$B=$ $\qquad$ Identify $\qquad$ points, then determine the period of the graph. NP= $\qquad$

$$
y=\ldots \cos (\ldots x)
$$

Use amplitude and new period to graph the equation.

Ex 4. $y=3 \cos \left(\frac{1}{2} x\right) \quad A=$ $\qquad$ $B=$ $\qquad$ Calculate New Period:

Where are 4 consecutive critical points?


Ex5. $y=-4 \cos$ Calculate New Period:

What intervals should you use on the $x$-axis? Where are 4 consecutive critical points? $B=$

$x-a x$
ints?


$$
y=A \sin [B(x-C)]+D \quad y=A \cos [B(x-C)]+D
$$

- Phase Shift (horizontal) --- represented by $\qquad$
- Vertical Shift --- represented by $\qquad$
Based on your knowledge of transformations, answer these questions about each equation.

6. $y=\sin (x-\pi / 4)$

- How is this graph transformed? $\qquad$
- What happens to the $x$-value? $\qquad$
- What about the $y$-value? $\qquad$
- Has the period changed? $\qquad$
- Has the maximum value changed? $\qquad$
- Has the minimum value changed? $\qquad$


7. $y=-\sin (x)+2$

- How is this graph transformed?
- What happens to the $x$-value? $\qquad$
- What about the $y$-value? $\qquad$
- Has the period changed? $\qquad$
- Has the maximum value changed? $\qquad$
- Has the minimum value changed? $\qquad$


8. $y=2 \cos (x+\pi / 2)-1$

- How is this graph transformed?
- What happens to the $x$-value? $\qquad$

- What about the $y$-value?
- Has the period changed? $\qquad$
- Has the maximum value changed? $\qquad$

- Has the minimum value changed?

9. $y=\cos (3 x)$

- How is this graph transformed? $\qquad$
- What happens to the $x$-value? $\qquad$
- What about the $y$-value? $\qquad$

- Has the period changed? $\qquad$ $N P=$ $\qquad$
- What are the new critical points? $\qquad$
- Has the maximum value changed? $\qquad$
- Has the minimum value changed?
* Use amplitude, new period, phase shift, and vertical shift to graph the equation.

Ex 10. $y=-2 \sin (2 x-\pi)+1 \quad$ must rewrite as $y=$ $\qquad$

$$
A=\ldots \quad C=\ldots \quad D=
$$

Amplitude $=$ $\qquad$ Reflect Across $x$-axis? $\qquad$ $N P=$ $\qquad$ Critical Pts $=$ $\qquad$

Phase Shift = $\qquad$ Vertical Shift = $\qquad$

> Assignment: PW \#1 Graphing Sine and Cosine PW \#2 Writing Equations of Sine and Cosine PW \#3 Graphing Sine and Cosine

