

Unit #6: Graphs and Inverses of Trig Functions

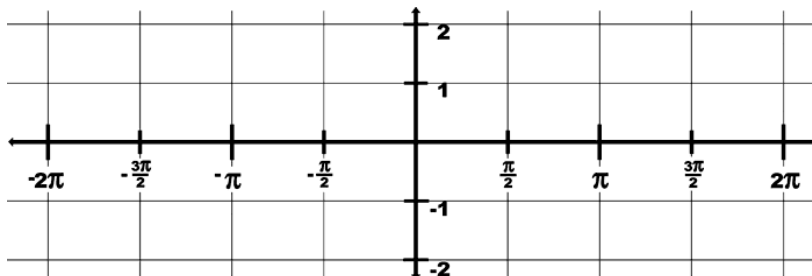
Lesson 5: Graphs of Secant and Cosecant

Complete the following tables. Remember you may convert $\sec(x)$ and $\csc(x)$ into decimal values if needed. Plot each point on the given coordinate plane. Connect continuous points to make a smooth curve. Mark any vertical asymptotes with a dotted vertical line. Do not connect any points across these asymptotes.

Graphing $f(x)=\sec(x)$

[Hint: Since sec is the reciprocal of cos, graph cos first.]

x	y=sec(x)	(x,y)
-2π	1	
$-7\pi/4$	$\sqrt{2}$	$(-7\pi/4, 1.4)$
$-3\pi/2$	Undefined	Vertical asymptote
$-5\pi/4$		
$-\pi$		
$-3\pi/4$		
$-\pi/2$		
$-\pi/4$		
0		
$\pi/4$		
$\pi/2$		
$3\pi/4$		
π		
$5\pi/4$		
$3\pi/2$		
$7\pi/4$		
2π		



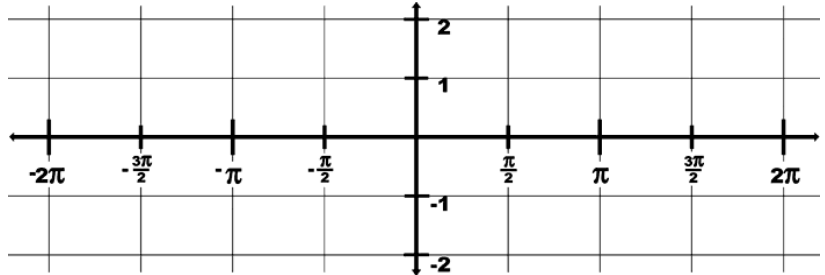
Facts to know about the graph of $\sec(x)$:

1. The domain is _____. Therefore you will have _____. List at least 4 asymptotes _____. They will occur every _____.
2. The range is _____.
3. Secant is symmetric to the _____. Therefore secant is an _____ function.
4. The secant function is periodic. It cycles every _____ or _____°.
5. Are there any x-intercepts? _____
6. Is there a y-intercept? _____

Graphing $f(x) = \csc(x)$

x	$y = \csc(x)$	Ordered pair (x,y)
-2π	undefined	Vertical asymptote
$-7\pi/4$	$\sqrt{2}$	$(-7\pi/4, 1.4)$
$-3\pi/2$	1	
$-5\pi/4$		
$-\pi$		
$-3\pi/4$		
$-\pi/2$		
$-\pi/4$		
0		
$\pi/4$		
$\pi/2$		
$3\pi/4$		
π		
$5\pi/4$		
$3\pi/2$		
$7\pi/4$		
2π		

[Hint: Since \csc is the reciprocal of \sin , graph \sin first.]



Facts to know about the graph of $\csc(x)$:

1. The domain is _____. Therefore you will have _____. List at least 4 asymptotes _____. They will occur every _____.
2. The range is _____.
3. Cosecant is symmetric to the _____. Therefore cosecant is an _____ function.
4. The cosecant function is periodic. It cycles every _____ or _____°.
5. Are there any x-intercepts? _____
6. Is there a y-intercept? _____

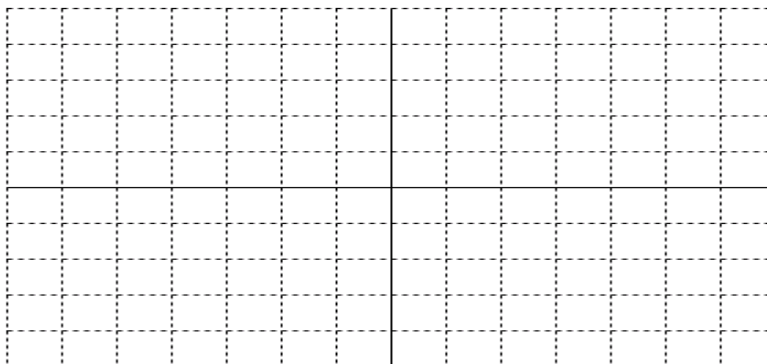
❖ Hint: When transforming secant and cosecant functions, you want to use the important points from the graph and transform those ordered pairs. Remember you only have to graph a full period of the function. After that you can use patterns to graph more than one.

Transformations of the Secant and Cosecant Functions

1. $y = \sec(x + \pi/4)$

- How is this graph transformed? _____
- What happens to the x-value? _____
- What about the y-value? _____
- Has the period changed? _____
- Have the asymptotes changed? _____

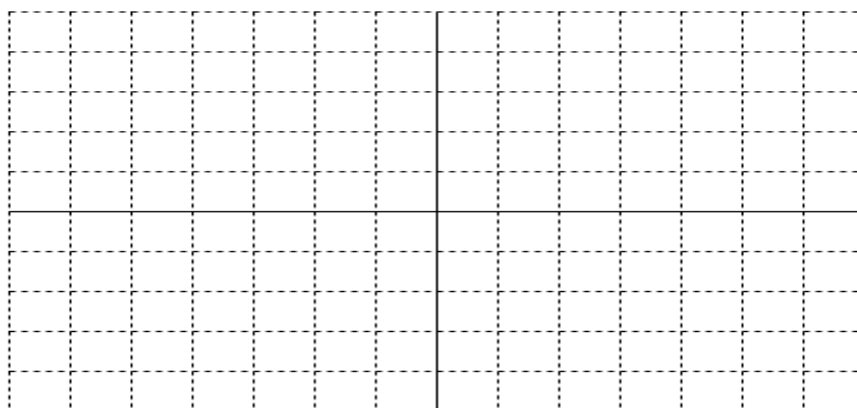
Sketch a graph of the transformed function



2. $y = \sec(2x)$

- How is this graph transformed? _____
- What happens to the x-value? _____
- What about the y-value? _____
- Has the period changed? _____
- Have the asymptotes changed? _____

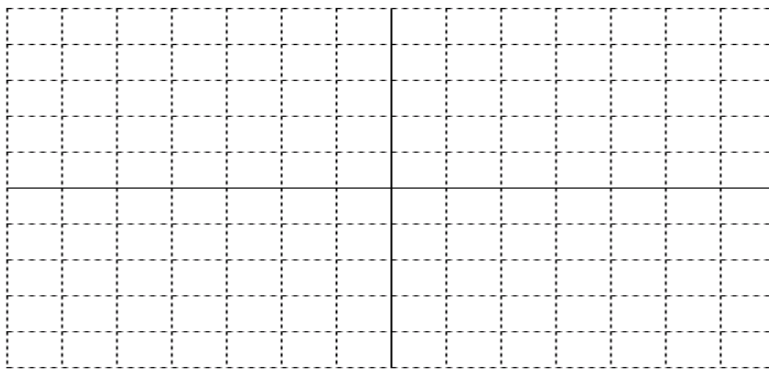
Sketch a graph of the transformed function



3. $y = -\csc(x) + 1$

- How is this graph transformed? _____
- What happens to the x-value? _____
- What about the y-value? _____
- Has the period changed? _____
- Have the asymptotes changed? _____

Sketch a graph of the transformed function



4. $y = \frac{1}{2} \csc(x)$

- How is this graph transformed? _____
- What happens to the x-value? _____
- What about the y-value? _____
- Has the period changed? _____
- Have the asymptotes changed? _____

Sketch a graph of the transformed function

