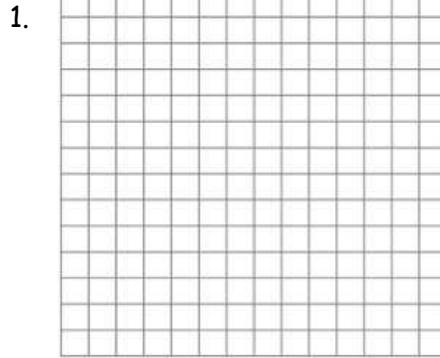
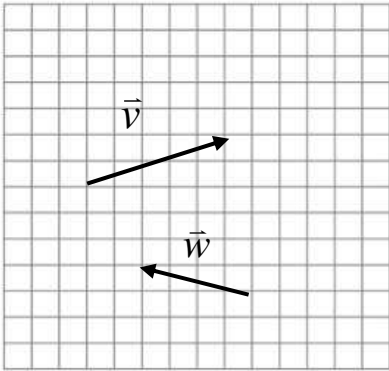
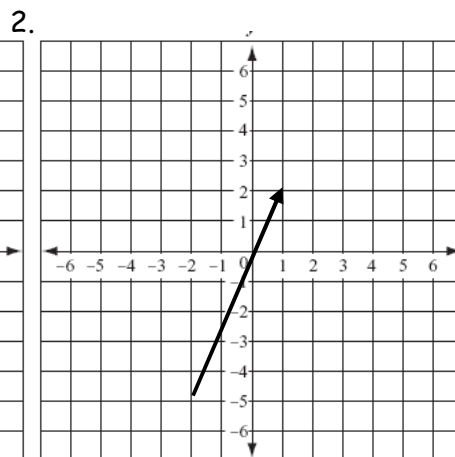
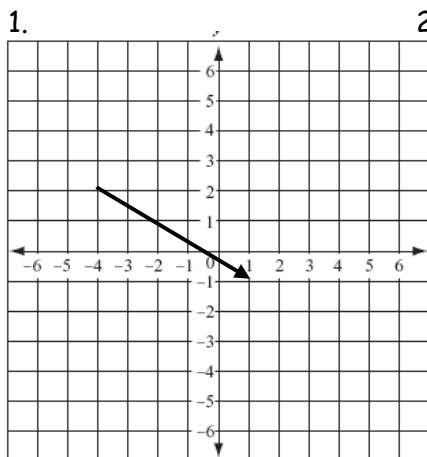


I. Use the diagram of vectors  $\mathbf{u}$  and  $\mathbf{v}$  to sketch the graph of 1)  $2\mathbf{v} + \mathbf{w}$  and 2)  $\mathbf{v} - 3\mathbf{w}$ .



II. Find the component form  $\langle a, b \rangle$  and magnitude of each vector  $\mathbf{v}$ .



3. initial pt:  $(-7, 3)$   
 terminal pt:  $(4, 1)$

4. initial pt:  $(-2, -4)$   
 terminal pt:  $(-5, 3)$

III. Write vectors #1 - 4 in Part II as a position vector in the form  $\mathbf{v} = ai + bj$ .

1.

2.

3.

4.

5. The component form  $\langle a, b \rangle$  of a vector represents a vector whose initial point is the \_\_\_\_\_.

IV. Find the magnitude of each vector.

1.  $\mathbf{v} = \langle 1, -2 \rangle$

2.  $\mathbf{v} = 4\mathbf{i} - 3\mathbf{j}$

3.  $\mathbf{v} = \langle 5, 3 \rangle$

4.  $\mathbf{v} = \mathbf{i} + \mathbf{j}$

5.  $\mathbf{v} = \left\langle \frac{3}{5}, \frac{4}{5} \right\rangle$

V. Find a unit vector,  $\mathbf{u}$ , in the direction of the given vector.

1.  $\mathbf{v} = 2\mathbf{i} + \mathbf{j}$

2.  $\mathbf{v} = \langle 3, 0 \rangle$

3.  $\mathbf{v} = \langle -5, 4 \rangle$

VI. Find a)  $\mathbf{u} + \mathbf{v}$       b)  $2\mathbf{u} - \mathbf{v}$       c)  $3\mathbf{u} - 2\mathbf{v}$

1.  $\mathbf{u} = \langle 2, -7 \rangle$   
 $\mathbf{v} = \langle 0, 3 \rangle$

2.  $\mathbf{u} = 2\mathbf{i} - 4\mathbf{j}$   
 $\mathbf{v} = \mathbf{i} + 5\mathbf{j}$

3.  $\mathbf{u} = \langle -3, -1 \rangle$   
 $\mathbf{v} = \langle -6, 0 \rangle$

VII. Find the magnitude and the direction angle of each vector. Give angles in decimal degrees to the nearest whole degree.

1.  $\mathbf{v} = \langle 1, -1 \rangle$

2.  $\mathbf{v} = \langle -3, \sqrt{3} \rangle$

3.  $\mathbf{v} = \langle -4\sqrt{2}, 4\sqrt{2} \rangle$

4.  $\mathbf{v} = \langle -3, -3 \rangle$

5.  $\mathbf{v} = \langle -8, 15 \rangle$

6.  $\mathbf{v} = \langle 6, 8 \rangle$

7.  $\mathbf{v} = \langle -5, 0 \rangle$

8.  $\mathbf{v} = \langle 0, 4 \rangle$

VIII. Find the component form  $\langle a, b \rangle$  of the vector,  $\mathbf{v}$ , given its magnitude and direction angle.

1.  $\theta = 30^\circ$   $\|\mathbf{v}\| = 24$

2.  $\theta = 84.7^\circ$   $\|\mathbf{v}\| = 52.9$

3.  $\theta = 60^\circ$   $\|\mathbf{v}\| = 80$

4.  $\theta = 45^\circ$   $\|\mathbf{v}\| = 5$

5.  $\theta = 136^\circ$   $\|\mathbf{v}\| = 7$

6.  $\theta = 210^\circ$   $\|\mathbf{v}\| = 6$

IX. Find the angle,  $\alpha$ , between the vectors.

1.  $\mathbf{v} = 2\mathbf{i} + \mathbf{j}$   
 $\mathbf{w} = -3\mathbf{i} - 4\mathbf{j}$

2.  $\mathbf{v} = \mathbf{i} + 3\mathbf{j}$   
 $\mathbf{w} = -2\mathbf{i} + 2\mathbf{j}$

3.  $\mathbf{v} = 6\mathbf{i} - \mathbf{j}$   
 $\mathbf{w} = -4\mathbf{i} - 2\mathbf{j}$

X. Vectors  $\mathbf{v}$  and  $\mathbf{w}$  represent two forces acting at the same point and  $\theta$  is the smallest positive angle between  $\mathbf{v}$  and  $\mathbf{w}$ . Find the magnitude (tenths) and direction angle (whole) of the resultant force.

1.  $\mathbf{w} = 40$  lbs.  
 $\mathbf{v} = 70$  lbs  
 $\theta = 45^\circ$

2.  $\mathbf{w} = 2$  kg  
 $\mathbf{v} = 8$  kg  
 $\theta = 120^\circ$

3.  $\mathbf{w} = 30$  lbs  
 $\mathbf{v} = 50$  lbs  
 $\theta = 150^\circ$