

I. Find the exact value for each under the specified conditions.

1. If $\sin \theta = \frac{1}{3}$, θ in quad II, find

a) $\sin\left(\theta + \frac{\pi}{6}\right)$

b) $\cos\left(\theta - \frac{\pi}{3}\right)$

c) $\tan\left(\theta + \frac{\pi}{4}\right)$

2. If $\cos \theta = \frac{1}{4}$, θ in quad IV, find

a) $\sin\left(\theta - \frac{\pi}{6}\right)$

b) $\cos\left(\theta + \frac{\pi}{3}\right)$

c) $\tan\left(\theta - \frac{\pi}{4}\right)$

II. Establish each identity.

3. $\sin\left(\frac{\pi}{2} + \theta\right) = \cos \theta$

4. $\cos(\pi - \theta) = -\cos \theta$

5. $\tan(2\pi - \theta) = -\tan \theta$

6. $\sin(\alpha + \beta) + \sin(\alpha - \beta) = 2 \sin \alpha \cos \beta$

7. $\frac{\sin(\alpha + \beta)}{\sin \alpha \cos \beta} = 1 + \cot \alpha \tan \beta$

8. $\frac{\cos(\alpha - \beta)}{\sin \alpha \cos \beta} = \cot \alpha + \tan \beta$