Unit #7: Trig Identities and Equations

for Sine, Cosine, and Tangent

- I. Find the exact value for each under the specified conditions.
- 1. If $\sin \theta = \frac{1}{3}$, θ in quad II, find

a)
$$\sin\left(\theta + \frac{\pi}{6}\right)$$

b)
$$\cos\left(\theta - \frac{\pi}{3}\right)$$

c)
$$\tan\left(\theta + \frac{\pi}{4}\right)$$

 $\cos \theta = \frac{1}{4}, \ \theta$ 2. If in quad IV, find

a)
$$\sin\left(\theta - \frac{\pi}{6}\right)$$

b)
$$\cos\left(\theta + \frac{\pi}{3}\right)$$

$$\tan\left(\theta-\frac{\pi}{4}\right)$$

II. Establish each identity.

$$3. \qquad \sin\left(\frac{\pi}{2} + \theta\right) = \cos\theta$$

$$4. \quad \cos(\pi-\theta)=-\cos\theta$$

$$5. \tan(2\pi - \theta) = -\tan\theta$$

6.
$$\sin(\alpha + \beta) + \sin(\alpha - \beta) = 2\sin\alpha\cos\beta$$

7.
$$\frac{\sin(\alpha + \beta)}{\sin\alpha\cos\beta} = 1 + \cot\alpha\tan\beta$$

8.
$$\frac{\cos(\alpha-\beta)}{\sin\alpha\cos\beta}=\cot\alpha+\tan\beta$$