## HW Answers Unit 5 Lesson 4 p. 310 Odds \#1-5, 11 - 23, 33 - 37

1. 


$\operatorname{adj}=\sqrt{5^{2}-3^{2}}=\sqrt{16}=4$

$$
\begin{array}{ll}
\sin \theta=\frac{\text { opp }}{\text { hyp }}=\frac{3}{5} & \csc \theta=\frac{\text { hyp }}{\text { opp }}=\frac{5}{3} \\
\cos \theta=\frac{\text { adj }}{\text { hyp }}=\frac{4}{5} & \sec \theta=\frac{\text { hyp }}{\text { adj }}=\frac{5}{4} \\
\tan \theta=\frac{\text { opp }}{\text { adj }}=\frac{3}{4} & \cot \theta=\frac{\text { adj }}{\text { opp }}=\frac{4}{3}
\end{array}
$$

3. 


hyp $=\sqrt{8^{2}+15^{2}}=17$
$\sin \theta=\frac{\text { opp }}{\text { hyp }}=\frac{8}{17}$
$\csc \theta=\frac{\text { hyp }}{\text { opp }}=\frac{17}{8}$
$\cos \theta=\frac{\text { adj }}{\text { hyp }}=\frac{15}{17}$
$\sec \theta=\frac{\text { hyp }}{\text { adj }}=\frac{17}{15}$
$\tan \theta=\frac{\mathrm{opp}}{\mathrm{adj}}=\frac{8}{15}$
$\cot \theta=\frac{\text { adj }}{\text { opp }}=\frac{15}{8}$
5.

hyp $=\sqrt{18^{2}+12^{2}}=\sqrt{468}=6 \sqrt{13}$
$\sin \theta=\frac{\text { opp }}{\text { hyp }}=\frac{18}{6 \sqrt{13}}=\frac{3}{\sqrt{13}}=\frac{3 \sqrt{13}}{13} \quad \csc \theta=\frac{\text { hyp }}{\text { opp }}=\frac{\sqrt{13}}{3}$
$\cos \theta=\frac{\text { adj }}{\text { hyp }}=\frac{12}{6 \sqrt{13}}=\frac{2}{\sqrt{13}}=\frac{2 \sqrt{13}}{13} \quad \sec \theta=\frac{\text { hyp }}{\text { adj }}=\frac{\sqrt{13}}{2}$
$\tan \theta=\frac{\mathrm{opp}}{\mathrm{adj}}=\frac{18}{12}=\frac{3}{2}$
$\cot \theta=\frac{\text { adj }}{\mathrm{opp}}=\frac{2}{3}$
11. Given: $\sin ^{-} \theta=\frac{5}{6}=\frac{\text { opp }}{\text { hyp }}$

$$
\begin{aligned}
& 5^{2}+(\mathrm{adj})^{2}=6^{2} \\
& \mathrm{adj}=\sqrt{11} \\
& \cos \theta=\frac{\sqrt{11}}{6} \\
& \tan \theta=\frac{5}{\sqrt{11}}=\frac{5 \sqrt{11}}{11} \\
& \cot \theta=\frac{\sqrt{11}}{5} \\
& \sec \theta=\frac{6}{\sqrt{11}}=\frac{6 \sqrt{11}}{11} \\
& \csc \theta=\frac{6}{5}
\end{aligned}
$$


15. Given: $\tan \theta=3=\frac{3}{1}=\frac{\text { opp }}{\text { adj }}$

$$
\begin{aligned}
3^{2}+1^{2} & =(\text { hyp })^{2} \\
\text { hyp } & =\sqrt{10}
\end{aligned}
$$

$\sin \theta=\frac{3 \sqrt{10}}{10}$
$\cos \theta=\frac{\sqrt{10}}{10}$
$\cot \theta=\frac{1}{3}$
$\sec \theta=\sqrt{10}$
$\csc \theta=\frac{\sqrt{10}}{3}$
13. Given: $\sec \theta=4=\frac{4}{1}=\frac{\text { hyp }}{\text { adj }}$

$$
\begin{aligned}
&(\mathrm{opp})^{2}+1^{2}=4^{2} \\
& \mathrm{opp}=\sqrt{15} \\
& \sin \theta=\frac{\sqrt{15}}{4}
\end{aligned}
$$

$\cos \theta=\frac{1}{4}$
$\tan \theta=\sqrt{15}$
$\cot \theta=\frac{1}{\sqrt{15}}=\frac{\sqrt{15}}{15}$
$\csc \theta=\frac{4}{\sqrt{15}}=\frac{4 \sqrt{15}}{15}$
17. Given: $\cot \theta=\frac{9}{4}=\frac{\text { adj }}{\text { hyp }}$

$$
4^{2}+9^{2}=(\mathrm{hyp})^{2}
$$

$$
\text { hyp }=\sqrt{97}
$$


$\sin \theta=\frac{4}{\sqrt{97}}=\frac{4 \sqrt{97}}{97}$
$\cos \theta=\frac{9}{\sqrt{97}}=\frac{9 \sqrt{97}}{97}$
$\tan \theta=\frac{4}{9}$
$\sec \theta=\frac{\sqrt{97}}{9}$
$\csc \theta=\frac{\sqrt{97}}{4}$
19. $\sin 60^{\circ}=\frac{\sqrt{3}}{2}, \cos 60^{\circ}=\frac{1}{2}$
(a) $\tan 60^{\circ}=\frac{\sin 60^{\circ}}{\cos 60^{\circ}}=\sqrt{3}$
(b) $\sin 30^{\circ}=\cos 60^{\circ}=\frac{1}{2}$
(c) $\cos 30^{\circ}=\sin 60^{\circ}=\frac{\sqrt{3}}{2}$
(d) $\cot 60^{\circ}=\frac{\cos 60^{\circ}}{\sin 60^{\circ}}=\frac{1}{\sqrt{3}}=\frac{\sqrt{3}}{3}$
23. $\cos \alpha=\frac{1}{4}$
(a) $\sec \alpha=\frac{1}{\cos \alpha}=4$
(b) $\sin ^{2} \alpha+\cos ^{2} \alpha=1$

$$
\begin{aligned}
\sin ^{2} \alpha+\left(\frac{1}{4}\right)^{2} & =1 \\
\sin ^{2} \alpha & =\frac{15}{16} \\
\sin \alpha & = \pm \frac{\sqrt{15}}{4}
\end{aligned}
$$

(c) $\cot \alpha=\frac{\cos \alpha}{\sin \alpha}= \pm \frac{1 / 4}{\sqrt{15} / 4}= \pm \frac{1}{\sqrt{15}}= \pm \frac{\sqrt{15}}{15}$
(d) $\sin \left(90^{\circ}-\alpha\right)=\cos \alpha=\frac{1}{4}$

$$
\text { (d) } \sin (90 \quad \alpha)-\cos u-4
$$

21. $\csc \theta=3, \sec \theta=\frac{3 \sqrt{2}}{4}$
(a) $\sin \theta=\frac{1}{\csc \theta}=\frac{1}{3}$
(b) $\cos \theta=\frac{1}{\sec \theta}=\frac{2 \sqrt{2}}{3}$
(c) $\tan \theta=\frac{\sin \theta}{\cos \theta}=\frac{1 / 3}{(2 \sqrt{2}) / 3}=\frac{\sqrt{2}}{4}$
(d) $\sec \left(90^{\circ}-\theta\right)=\csc \theta=3$
22. (a) $\cos 60^{\circ}=\frac{1}{2}$
(b) $\tan \frac{\pi}{6}=\frac{1}{\sqrt{3}}=\frac{\sqrt{3}}{3}$

23. (a) $\cot \frac{\pi}{4}=\cot 45^{\circ}=1$
(b) $\cos 45^{\circ}=\frac{1}{\sqrt{2}}=\frac{\sqrt{2}}{2}$

24. (a) $\cos \frac{\pi}{6}=\cos 30^{\circ}=\frac{\sqrt{3}}{2}$
(b) $\sec 60^{\circ}=\frac{1}{\cos 60^{\circ}}=2$
