

In class practice problems: Hyperbolas (part 2)

$$\textcircled{1} \frac{(x-1)^2}{9} - \frac{(y-3)^2}{4} = 1 \quad C: (1, 3) \quad V: (-2, 3) (4, 3)$$

$$9 + 4 = c^2$$

$$13 = c^2$$

$$\pm \sqrt{13} = c$$

$$CV: (1, 1) (1, 5)$$

$$F: (1 \pm \sqrt{13}, 3)$$

$$\text{Asym: } y = \frac{2}{3}x + \frac{7}{3}$$

$$y = -\frac{2}{3}x + \frac{11}{3}$$

$$\textcircled{2} \frac{(y-3)^2}{9} - \frac{(x+2)^2}{1} = 1 \quad C: (-2, 3) \quad V: (-2, 0) (-2, 6)$$

$$9 + 1 = c^2$$

$$10 = c^2$$

$$\pm \sqrt{10} = c$$

$$CV: (-3, 3) (-1, 3)$$

$$F: (-2, 3 \pm \sqrt{10})$$

$$\text{Asym: } y = 3x + 9$$

$$y = -3x - 3$$

$$\textcircled{3} \frac{(y-2)^2}{5} - \frac{(x-2)^2}{3} = 1 \quad C: (2, 2) \quad V: (2, 2 \pm \sqrt{5})$$

$$5 + 3 = c^2$$

$$8 = c^2$$

$$\pm \sqrt{8} = c$$

$$\pm 2\sqrt{2} = c$$

$$CV: (2 \pm \sqrt{3}, 2)$$

$$F: (2, 2 \pm 2\sqrt{2})$$

$$\text{Asym: } y - 2 = \pm \frac{\sqrt{15}}{5} (x - 2)$$

$$\text{or } y = \pm \frac{\sqrt{15}}{5} (x - 2) + 2$$